Please check the examination details below before entering your candidate information

Candidate surname	Other names
Solved by Mr. Pabitra	

Centre Number | Candidate Number

Pearson Edexcel International GCSE

Monday 3 June 2024

Morning (Time: 2 hours)

Paper reference **4MA1/2H**

Mathematics A

PAPER 2H

Higher Tier

Solved by Mr. Pabitra



You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
  – *there may be more space than you need.*
- **Calculators may be used.**
- You must **NOT** write anything on the formulae page.
- Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
  – *use this as a guide as to how much time to spend on each question.*

Advice

Solved by Mr. Pabitra | Math Tonic

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over

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International GCSE Mathematics

Formulae sheet – Higher Tier

Arithmetic series

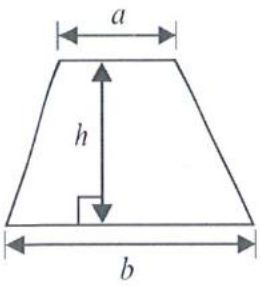
Sum to n terms, $S_n = \frac{n}{2}[2a + (n-1)d]$

The quadratic equation

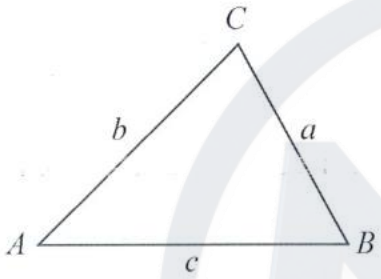
The solutions of $ax^2 + bx + c = 0$ where $a \neq 0$ are given by:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Area of trapezium $= \frac{1}{2}(a+b)h$



Trigonometry



In any triangle ABC

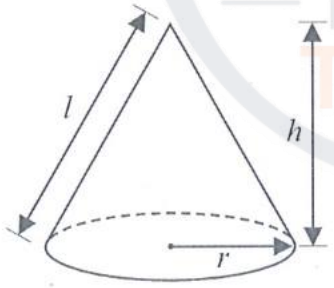
Sine Rule $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine Rule $a^2 = b^2 + c^2 - 2bc\cos A$

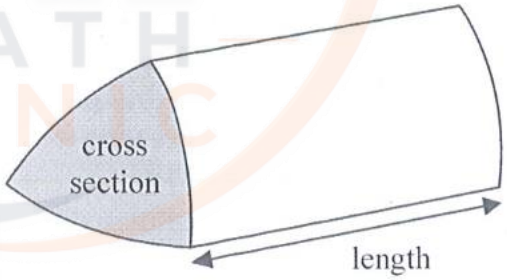
Area of triangle $= \frac{1}{2}ab\sin C$

Volume of cone $= \frac{1}{3}\pi r^2 h$

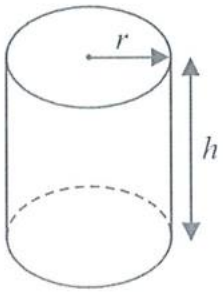
Curved surface area of cone $= \pi r l$



Volume of prism
= area of cross section × length

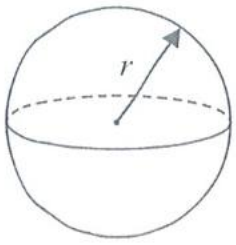


Volume of cylinder $= \pi r^2 h$
Curved surface area of cylinder $= 2\pi r h$



Volume of sphere $= \frac{4}{3}\pi r^3$

Surface area of sphere $= 4\pi r^2$



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Solved by Mr. Pabitra

P 7 3 9 9 4 A 0 2 2 8

Answer ALL TWENTY FIVE questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 Here are eight numbers written in order of size

h	6	7	8	j	16	k	k

where h, j and k are integers.

The median of the eight numbers is 10

The mode of the eight numbers is 18

The range of the eight numbers is 13

Work out the value of h, the value of j and the value of k

$K = 18$

Range $= 13$

$18 - h = 13$

$h = 18 - 13$

$h = 5$

$\frac{8+j}{2} = 10$

$8 + j = 20$

$j = 20 - 8$

$j = 12$

$h =$ 5

$j =$ 12

$k =$ 18

(Total for Question 1 is 3 marks)

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Solved by Mr. Pabitra

2 (a) On the grid, draw the straight line with equation

(i) $y = 2$

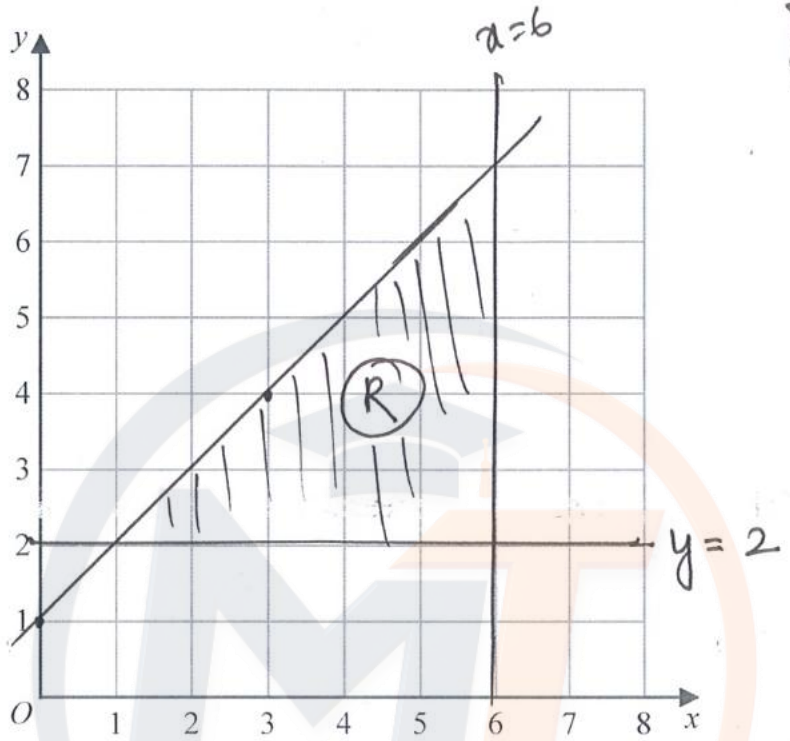
(ii) $x = 6$

(iii) $y = x + 1$

Label each line with its equation.

$y = x + 1$

x	0	3
y	1	4



(3)

(b) Show, by shading on the grid, the region that satisfies all three of the inequalities

$y \geqslant 2$ $x \leqslant 6$ $y \leqslant x + 1$

Label the region **R**

(1)

(Total for Question 2 is 4 marks)

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Solved by Mr. Pabitra

3 A plane takes 9 hours 36 minutes to fly from New Delhi to Perth.

The plane flies at an average speed of 820 km/h.

Work out the total distance the plane flies.

Total Distance = Average Speed × Time

= 820 km/hr × 9.6 hr

Time = 9 hr 36 min

$= 9 + \frac{36}{60}$

$= 9 + \frac{3}{5}$

$= 9 + 0.6$

$= 9.6$ hr

= 7872 km

km

(Total for Question 3 is 3 marks)

4 Show that $2\frac{4}{7} \times 3\frac{1}{9} = 8$

$\frac{\cancel{18}^{2}}{\cancel{7}_{1}} \times \frac{\cancel{28}^{4}}{\cancel{9}_{1}}$

$\frac{2 \times 4}{1 \times 1} = \frac{8}{1} = 8$

(Total for Question 4 is 3 marks)

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MATH TONIC

Solved by Mr. Pabitra

5 The diagram shows triangle ABC

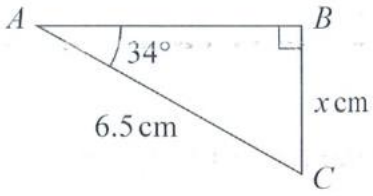


Diagram **NOT** accurately drawn

Work out the value of x
Give your answer correct to one decimal place.

$\sin\theta = \frac{opp}{hyp}$

$x = 6.5 \times \sin 34$

$x = 3.6\text{ cm}$

$x =$ 3.6cm

(Total for Question 5 is 3 marks)

6 Change a speed of w metres per second to a speed in kilometres per hour.
Give your answer in terms of w in its simplest form.

$1\ \frac{km}{hr} = \frac{1000\ m}{3600\ s}$

$1\ km/hr = \frac{5}{18}\ m/s$

$1\ m/s = \frac{18}{5}\ km/hr$

$w\ \frac{m}{s} = w \times \frac{18}{5}\ km/hr$

$= 3.6w\ km/hr$

3.6w kilometres per hour

(Total for Question 6 is 3 marks)

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Solved by Mr. Pabitra

7 The diagram shows a 6-sided shape $ABCDEF$

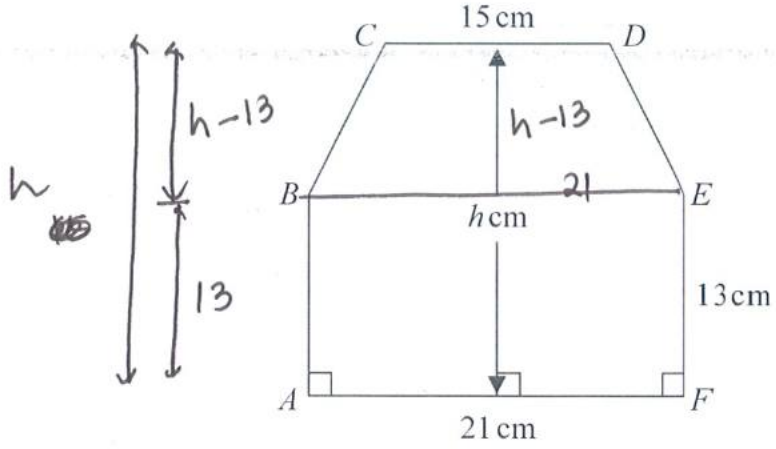


Diagram **NOT** accurately drawn

$AF = 21$ cm $\quad CD = 15$ cm $\quad AB = FE = 13$ cm

The perpendicular height of the shape is h cm
CD is parallel to AF

The area of the shape is 390 cm^2

Work out the value of h

Area of Rectangle + Area of Trapezium = 390

$$(13 \times 21) + \frac{(15+21)(h-13)}{2} = 390$$

$$273 + \frac{36(h-13)}{2} = 390$$

$$18(h-13) = 390 - 273$$

$$18(h-13) = 117$$

$$h - 13 = \frac{117}{18} = 6.5$$

$$h = 6.5 + 13$$

$$\boxed{h = 19.5}$$

$h =$ 19.5 cm

(Total for Question 7 is 4 marks)

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Solved by Mr. Pabitra

8 Ishir plants 600 bulbs in a garden.
He plants tulip bulbs, crocus bulbs and daffodil bulbs so that

number of tulip bulbs : number of crocus bulbs : number of daffodil bulbs = 9 : 4 : 2

45% of the tulip bulbs are for yellow flowers.

$\frac{5}{8}$ of the crocus bulbs are for yellow flowers.

All of the daffodil bulbs are for yellow flowers.

Work out the number of bulbs that are for yellow flowers.

Tulip bulbs: $\frac{9}{15} \times 600 = 360$

T : C : D

9 : 4 : 2

$\frac{9}{15}$ $\frac{4}{15}$ $\frac{2}{15}$

Crocus bulbs $\frac{4}{15} \times 600 = 160$

Daffodil bulbs

$\frac{2}{15} \times 600 = 80$ (All are yellow)

Yellow Tulip: $\frac{45}{100} \times 360 = 162$

Yellow Crocus: $\frac{5}{8} \times 160 = 100$

Total Yellow: $162 + 100 + 80 = 342$

342

(Total for Question 8 is 5 marks)

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Solved by Mr. Pabitra

9 Giovanni invests 4500 koruna in a savings account for 4 years.
He gets 2.4% per year compound interest.

Work out how much money Giovanni will have in the savings account at the end of 4 years.
Give your answer correct to the nearest koruna.

$P\left(1+\frac{r}{100}\right)^5$

$4500 \times \left(1+\frac{2.4}{100}\right)^4$

4947.8

4948

4948 koruna

(Total for Question 9 is 3 marks)

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Solved by Mr. Pabitra

10 Solve the simultaneous equations

$$6x + 4y = 1 \quad \text{(i)}$$
$$3x + 5y = 8 \quad \text{(ii)}$$

Show clear algebraic working.

(i) $\Longrightarrow$ $6x + 4y = 1$

(ii) $\times 2$ $\Longrightarrow$ $6x + 10y = 16$

$-6y = -15$

$y = 15/6$

$\boxed{y = 5/2}$

$6x + 4y = 1$

$6x + 4 \times 5/2 = 1$

$6x + 10 = 1$

$6x = 1 - 10$

$6x = -9$

$x = -9/6 = -3/2$

$x = \dfrac{5}{2} = 2.5$

$y = \dfrac{-3}{2} = -1.5$

(Total for Question 10 is 3 marks)

11 (i) Factorise $x^2 + 9x - 22$

$11 \times -2 = -22$

$11 - 2 = 9$

$(x + 11)(x - 2)$

(2)

(ii) Hence, solve $x^2 + 9x - 22 = 0$

$(x + 11)(x - 2) = 0$

$x + 11 = 0$ $\qquad$ $x - 2 = 0$

$\boxed{x = -11}$ $\qquad$ $\boxed{x = 2}$

$x = -11, 2$

(1)

(Total for Question 11 is 3 marks)

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MATH TONIC

Solved by Mr. Pabitra

12 Ali uses a fitness tracker to count the number of steps he walks each day for 7 days.

For the first 4 days, his mean number of steps is 11 800
For the next 3 days, his mean number of steps is 13 207

Work out his mean number of steps for the 7 days.

$$\frac{\text{Sum of steps for 4 days}}{4} = 11800$$

\# Sum of steps for 4 days $= 4 \times 11800 = 47{,}200$

$$\frac{\text{Sum of steps for next 3 days}}{3} = 13207$$

\# Sum of steps for next 3 days $= 3 \times 13207 = 39621$

$$\frac{47200 + 39621}{7} = 12403$$

12403

(Total for Question 12 is 3 marks)

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MATH TONIC

Solved by Mr. Pabitra

13 The table gives information about the distances, in km, that 70 teachers travel to school.

Distance (d km)	Frequency
$0 < d \leqslant 10$	7
$10 < d \leqslant 20$	17
$20 < d \leqslant 30$	18
$30 < d \leqslant 40$	14
$40 < d \leqslant 50$	10
$50 < d \leqslant 60$	4

(a) Complete the cumulative frequency table.

Distance (d km)	Cumulative frequency
$0 < d \leqslant 10$	7
$0 < d \leqslant 20$	7+17 = 24
$0 < d \leqslant 30$	24+18 = 42
$0 < d \leqslant 40$	42+14 = 56
$0 < d \leqslant 50$	56+10 = 66
$0 < d \leqslant 60$	66+4 = 70

(1)

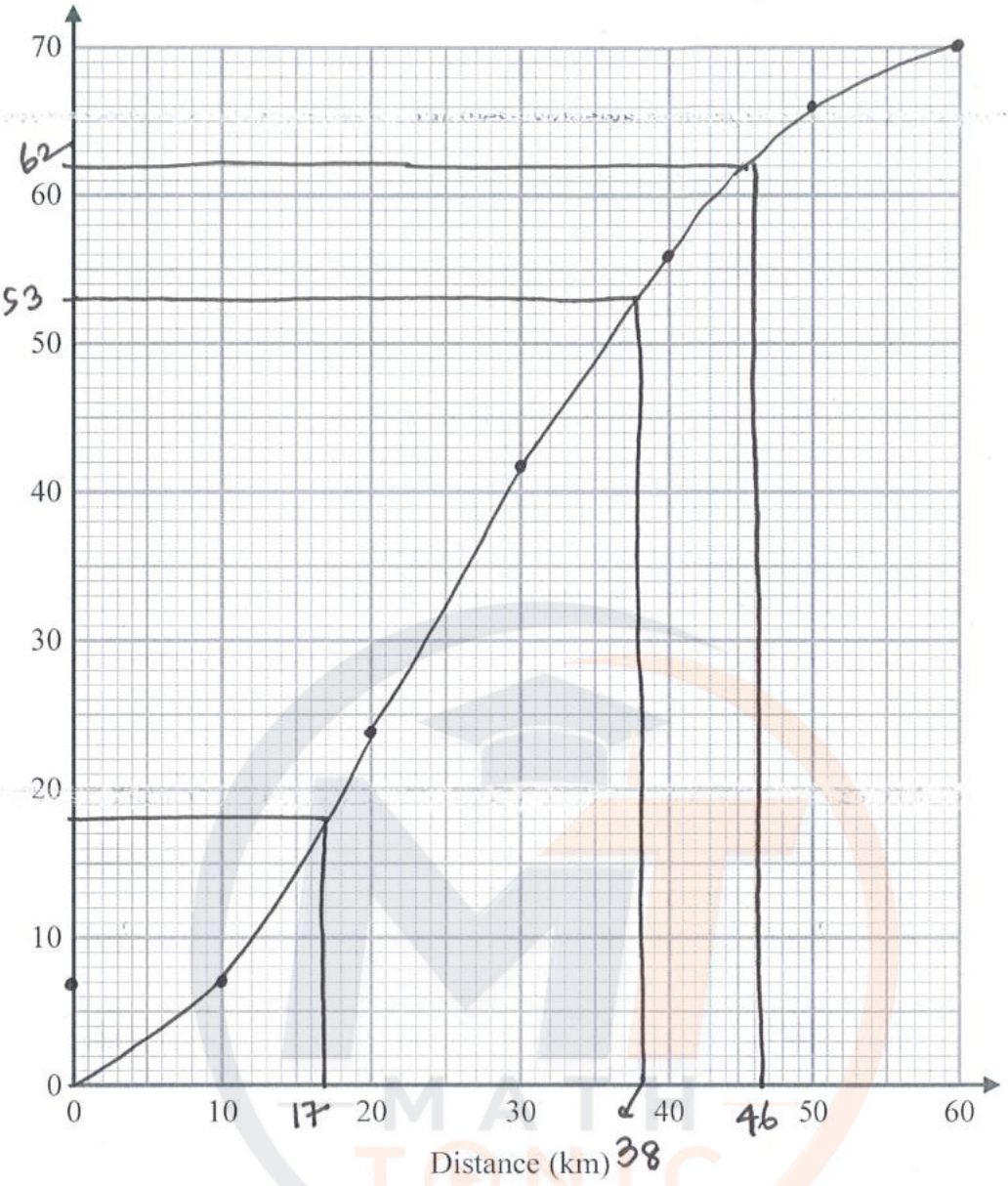
(b) On the grid opposite, draw a cumulative frequency graph for your table.

(2)

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Solved by Mr. Pabitra

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(c) Use your graph to find an estimate for the interquartile range of the distances.

$IQR = Q_3 - Q_1$

$(3/4 \times 70)^{th} - (1/4 \times 70)^{th}$

$(52.5)^{th} - 17.5^{th}$

$53^{rd} - 18^{th}$

$38 - 17$

21 km

(2)

(d) Use your graph to find an estimate for the number of teachers who travel more than 46 km.

$70 - 62 = 8$

8

(2)

(Total for Question 13 is 7 marks)

Solved by Mr. Pabitra

14 (a) Show that $3y(2y + 5)(y + 7)$ can be written in the form $ay^3 + by^2 + cy$ where a, b and c are integers.

$3y(2y^2 + 14y + 5y + 35)$

$3y(2y^2 + 19y + 35)$

$6y^3 + 57y^2 + 105y$

$a = 6 \quad b = 57 \quad c = 105$

(3)

(b) Solve $\frac{2x + 3}{5} + \frac{6x - 5}{4} = \frac{163}{100}$

Show clear algebraic working.

$\frac{4(2x+3) + 5(6x-5)}{5 \times 4} = \frac{163}{100}$

$\frac{8x + 12 + 30x - 25}{20} = \frac{163}{100}$

$\frac{38x - 13}{20} = \frac{163}{100}$

$100(38x - 13) = 20 \times 163$

$3800x - 1300 = 3260$

$3800x = 3260 + 1300$

$3800x = 4560$

$x = \frac{4560}{3800}$

$\boxed{x = 1.2}$

$x =$ 1.2

(4)

(Total for Question 14 is 7 marks)

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MATH TONIC

Solved by Mr. Pabitra

15 (a) Make g the subject of $e = \sqrt{\dfrac{7g+5}{11+2g}}$

$$e^2 = \frac{7g+5}{11+2g}$$

$$e^2(11+2g) = 7g+5$$

$$11e^2 + 2ge^2 = 7g+5$$

$$2ge^2 - 7g = 5 - 11e^2$$

$$g(2e^2-7) = 5-11e^2$$

$$g = \frac{5-11e^2}{2e^2-7}$$

$$\boxed{g = \frac{5-11e^2}{2e^2-7}}$$

(4)

(b) Solve the inequality $3y^2 + 4y - 32 > 0$
Show your working clearly.

$$3y^2+4y-32 > 0$$



$$\boxed{x > 8/3 \text{ and } x < -4}$$

$$3y^2+4y-32 = 0$$

$3 \times 32 = -96$

$12 \times -8 = -96$

$12 - 8 = 4$

$(3y+12)(3y-8) = 0$

$(y+4)(3y-8) = 0$

$y+4=0 \quad 3y-8=0$

$y=-4 \quad 3y=8$

$y = 8/3$

(3)

(Total for Question 15 is 7 marks)

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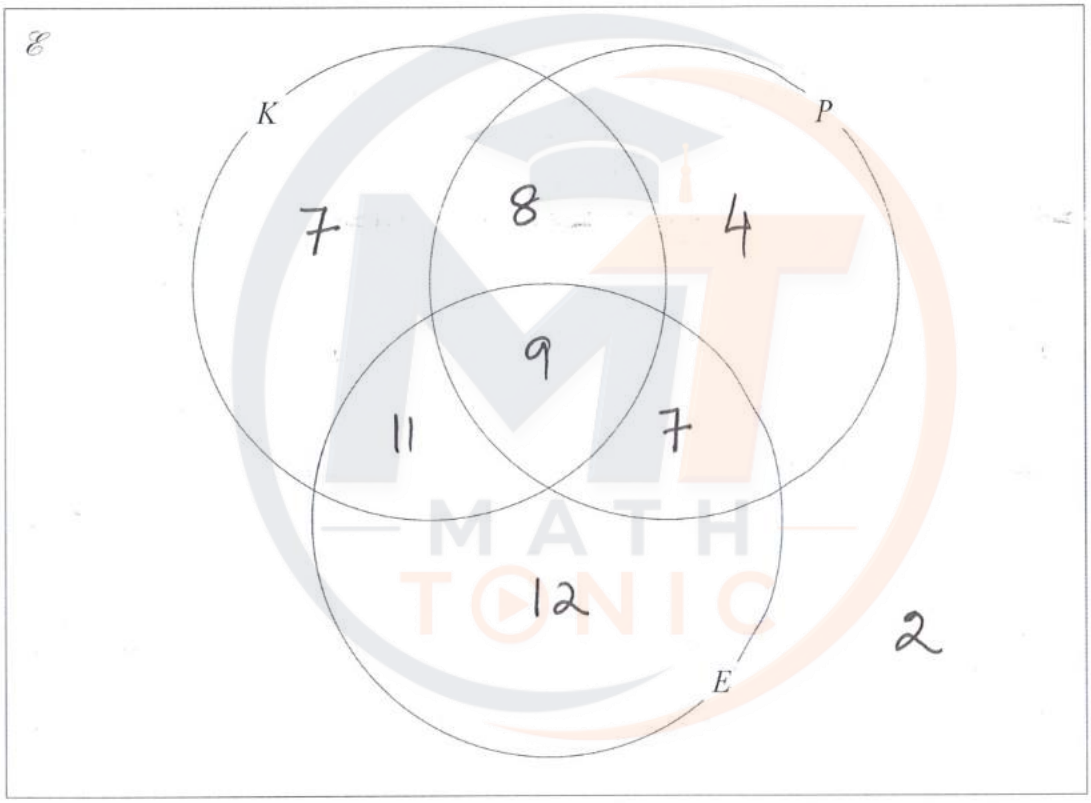
Solved by Mr. Pabitra

16 60 art students were asked if they would like to attend workshops for knitting (K), for photography (P) or for embroidery (E)

Of these students

9 chose knitting, photography and embroidery
17 chose knitting and photography
16 chose photography and embroidery
20 chose knitting and embroidery
28 chose photography
39 chose embroidery
2 chose none of the workshops

(a) Using this information, complete the Venn diagram to show the numbers of students in each subset.



(3)

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Solved by Mr. Pabitra

One of the students is chosen at random.

Given that this student chose photography,

(b) find the probability that this student also chose knitting.

$$\frac{8+9}{8+9+4+7}$$

$\frac{17}{28}$

(2)

(c) Find $n(P \cap K')$

$4+7=11$

11

(1)

(d) Find $n([P \cup E] \cap K)$

$8+9+11=28$

28

(1)

(Total for Question 16 is 7 marks)

17 Q is directly proportional to the square root of d

$Q = 4.5$ when $d = 324$

Find a formula for Q in terms of d

$Q \propto \sqrt{d}$

$Q = K \times \sqrt{d}$

$4.5 = K \times \sqrt{324}$

$4.5 = K \times 18$

$K = \frac{4.5}{18}$

$K = 0.25$

$Q = 0.25\sqrt{d}$

$Q = 0.25\sqrt{d}$

(Total for Question 17 is 3 marks)

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MATH TONIC
Solved by Mr. Pabitra

18 The straight line **P** has equation $5y + 2x = 7$

Find the gradient of a straight line that is perpendicular to **P**

$5y + 2x = 7$

$5y = -2x + 7$

$y = \frac{-2}{5}x + \frac{7}{5}$

gradient $(m_1) = -2/5$

for Perpendicular

$m_1 \times m_2 = -1$

$-2/5 \times m_2 = -1$

$\boxed{m_2 = 5/2}$

5/2

(Total for Question 18 is 2 marks)

19 $G = \dfrac{c}{2f - 3h}$

$c = 8$ correct to the nearest whole number
$f = 6.62$ correct to 2 decimal places
$h = 1.2$ correct to 1 decimal place

Work out the lower bound for the value of G
Give your answer correct to 3 decimal places.
Show your working clearly.

LB		UB
7.5	$C = 8$	8.5
6.615	$f = 6.62$	6.625
1.15	$h = 1.2$	1.25

$LB = \dfrac{LB}{UB} = \dfrac{LB}{UB - LB}$

$G_{LB} = \dfrac{C_{LB}}{2 \times f_{UB} - 3 \times h_{LB}}$

$G_{LB} = \dfrac{7.5}{2 \times 6.625 - 3 \times 1.15}$

$G_{LB} = \dfrac{7.5}{9.8}$

$\boxed{G_{LB} = 0.765}$

$\boxed{0.765}$

(Total for Question 19 is 3 marks)

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Solved by Mr. Pabitra

20 Given that $k = x - y$ and $x = \frac{1}{4y}$

express $\frac{5k}{x+2}$ in the form $\frac{a - by^2}{c + dy}$ where a, b, c and d are integers.

$$\frac{5(x-y)}{x+2} = \frac{5\left(\frac{1}{4y} - y\right)}{\frac{1}{4y} + 2}$$

$$\frac{5\left[\frac{1-4y^2}{4y}\right]}{\left[\frac{1+8y}{4y}\right]}$$

$$\frac{5(1-4y^2)}{\cancel{4y}} \div \frac{1+8y}{\cancel{4y}}$$

$$\frac{5(1-4y^2)}{1+8y}$$

$$\boxed{\frac{5-20y^2}{1+8y}}$$

$\frac{1}{4y} - \frac{y}{1}$

$\frac{1\times1 - y\times4y}{4y\times1}$

$\frac{1-4y^2}{4y}$

$\frac{1}{4y} + \frac{2}{1}$

$\frac{1\times1 + 2\times4y}{4y\times1}$

$\frac{1+8y}{4y}$

Ex: $\frac{\frac{a}{b}}{\frac{c}{b}}$

$\frac{a}{b} \div \frac{c}{b}$

$\frac{a}{\cancel{b}} \times \frac{\cancel{b}}{c} = \frac{a}{c}$

(Total for Question 20 is 3 marks)

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Solved by Mr. Pabitra

21 The diagram shows a square $ABCD$ and a circle.

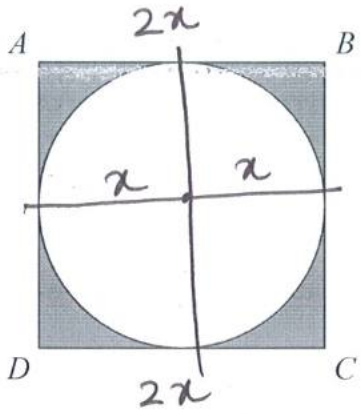


Diagram **NOT** accurately drawn

The sides of the square are tangents to the circle.

The total area of the shaded regions is $80\,cm^2$

Work out the length of AC
Give your answer correct to 3 significant figures.

Let $AB = 2x$

then $MB = x$

Area of Square $= 2x \times 2x = 4x^2$

Area of Circle $= \pi r^2 = \pi x^2$

Area of Square − Area of Circle = Area of shaded

$$4x^2 - \pi x^2 = 80$$

$$x^2(4-\pi) = 80$$

$$x^2 = \frac{80}{4-\pi}$$

$$x = \sqrt{\frac{80}{4-\pi}} = 9.65\,cm$$

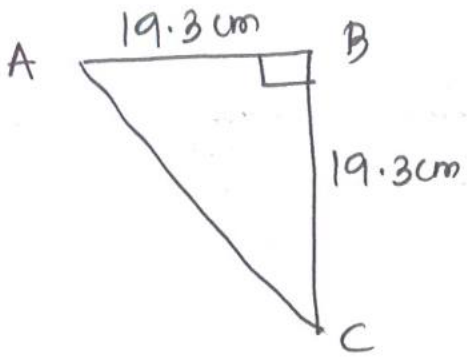
Radius $= 9.65\,cm$

Diameter $= 2 \times 9.65 = 19.3\,cm$

$AB = 19.3\,cm$

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Solved by Mr. Pabitra



$$Ac = \sqrt{AB^2 + BC^2}$$

$$= \sqrt{19.3^2 + 19.3^2}$$

$$= \sqrt{744.98}$$

$$\boxed{Ac = 27.3\text{ cm}}$$

27.3 cm

(Total for Question 21 is 5 marks)

Turn over for Question 22

DO NOT WRITE IN THIS AREA
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Solved by Mr. Pabitra

22 The straight line **L** has equation $x + y = 5$

The curve **C** has equation $2x^2 + 3y^2 = 210$

Find the coordinates of the points where **L** and **C** intersect.
Show clear algebraic working.

$x + y = 5$

$y = 5 - x$

$2x^2 + 3y^2 = 210$

$2x^2 + 3(5-x)^2 = 210$

$2x^2 + 3(25 - 10x + x^2) = 210$

$2x^2 + 75 - 30x + 3x^2 = 210$

$5x^2 - 30x + 75 - 210 = 0$

$5x^2 - 30x - 135 = 0$

$x^2 - 6x - 27 = 0$

$(x-9)(x+3) = 0$

$x - 9 = 0$ | $x + 3 = 0$

$\boxed{x = 9}$ | $\boxed{x = -3}$

$y = 5 - x$ | $y = 5 - x$

$y = 5 - 9$ | $y = 5 - (-3)$

$\boxed{y = -4}$ | $\boxed{y = 8}$

(9 , −4) (−3 , 8)

(Total for Question 22 is 5 marks)

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P 7 3 9 9 4 A 0 2 2 2 8

23 Simplify $\dfrac{30 \times 25^{2x+7}}{\sqrt{180} \times \left(\sqrt{5}\right)^{4x+9}}$

Give your answer in the form 5^w where w is an expression in terms of x
Show each stage of your working clearly.

$$\frac{2 \times 3 \times 5 \times (5^2)^{2x+7}}{6\sqrt{5} \times (\sqrt{5})^{4x+9}}$$

$$\frac{6 \times 5^1 \times 5^{4x+14}}{6 \times 5^{1/2} \times (5^{1/2})^{4x+9}}$$

$$\frac{5^{1+4x+14}}{5^{1/2} \times 5^{2x+9/2}}$$

$$\frac{5^{4x+15}}{5^{1/2+9/2+2x}} = \frac{5^{4x+15}}{5^{2x+5}}$$

$$= 5^{4x+15-(2x+5)}$$

$$= 5^{4x+15-2x-5} = 5^{2x+10}$$

$$5^{2x+10}$$

$\sqrt{180}$
$\sqrt{9 \times 4 \times 5}$
$\sqrt{9} \times \sqrt{4} \times \sqrt{5}$
$3 \times 2 \times \sqrt{5}$
$6\sqrt{5}$
$6 \times 5^{1/2}$

(Total for Question 23 is 3 marks)

Turn over for Question 24

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24

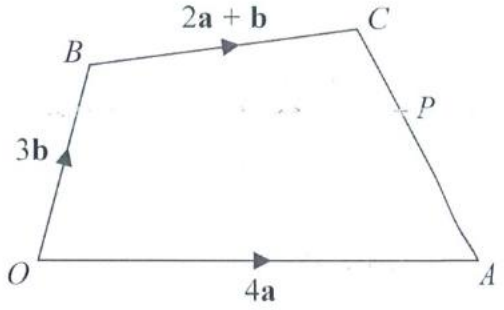


Diagram **NOT** accurately drawn

The diagram shows a quadrilateral $OACB$ in which

$\overrightarrow{OA} = 4\mathbf{a}$ $\overrightarrow{OB} = 3\mathbf{b}$ $\overrightarrow{BC} = 2\mathbf{a} + \mathbf{b}$

(a) Find $\overrightarrow{AC}$ in terms of **a** and **b**
Give your answer in its simplest form.

$\overrightarrow{AC} = \overrightarrow{AO} + \overrightarrow{OB} + \overrightarrow{BC}$

$\overrightarrow{AC} = -4a + 3b + 2a + b$

$\overrightarrow{AC} = -2a + 4b$

$\overrightarrow{AC} =$ $-2a+4b$

(2)

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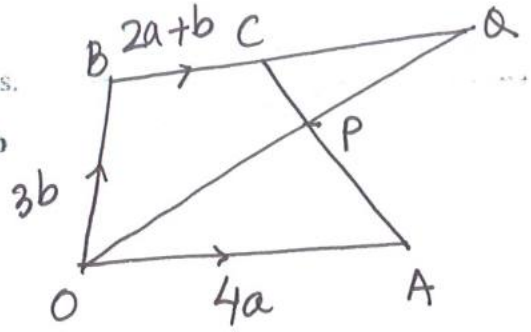
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The point P lies on AC such that $AP : PC = 3 : 2$

The point Q is such that OPQ and BCQ are straight lines.

(b) Using a vector method, find $\overrightarrow{OQ}$ in terms of **a** and **b**
Give your answer in its simplest form.
Show your working clearly.



$\overrightarrow{AC} = -2a+4b$

$\overrightarrow{AP} = \frac{3}{5} \times \overrightarrow{AC}$

$\overrightarrow{AP} = \frac{3}{5} \times (-2a+4b)$

$\overrightarrow{PC} = \frac{2}{5} \times (-2a+4b)$

$\overrightarrow{OP} = \overrightarrow{OA} + \overrightarrow{AP}$

$\overrightarrow{OP} = 4a + \frac{3}{5}(-2a+4b)$

$\overrightarrow{OP} = 4a - \frac{6}{5}a + \frac{12}{5}b$

$\overrightarrow{OP} = \frac{14}{5}a + \frac{12}{5}b$

$\overrightarrow{OQ}$ is multiple of $\overrightarrow{OP}$

$\overrightarrow{OQ} = m \times \overrightarrow{OP}$

$\overrightarrow{OQ} = m\left[\frac{14}{5}a + \frac{12}{5}b\right]$

$\boxed{\overrightarrow{OQ} = \frac{14}{5}ma + \frac{12}{5}mb}$ (i)

$AP : PC$

$3 : 2$

$\overrightarrow{AP} = \frac{3}{5}\overrightarrow{AC}$

$\overrightarrow{PC} = \frac{2}{5}\overrightarrow{AC}$

$\overrightarrow{OQ} = \overrightarrow{OB} + \overrightarrow{BQ}$

$\overrightarrow{OQ} = \overrightarrow{OB} + n \times \overrightarrow{BC}$

$\overrightarrow{OQ} = 3b + n(2a+b)$

$\boxed{\overrightarrow{OQ} = 3b + 2na + nb}$ (ii)

Equⁿ (i) and (ii) are equal

$3b + 2na + nb = \frac{14}{5}ma + \frac{12}{5}mb$

$2na + (3+n)b = \frac{14}{5}ma + \frac{12}{5}mb$

$2n = \frac{14}{5}m$

$n = \frac{14}{10}m$

$3 + n = \frac{12}{5}m$

$3 + \frac{14}{10}m = \frac{12}{5}m$

$\frac{14}{10}m - \frac{12}{5}m = -3$

$-\frac{10}{10}m = -3$

$-m = -3$

$m = 3$

$\overrightarrow{OQ} = \frac{14}{5} \times 3a + \frac{12}{5} \times 3b$

$\overrightarrow{OQ} = \boxed{\frac{42}{5}a + \frac{36}{5}b}$

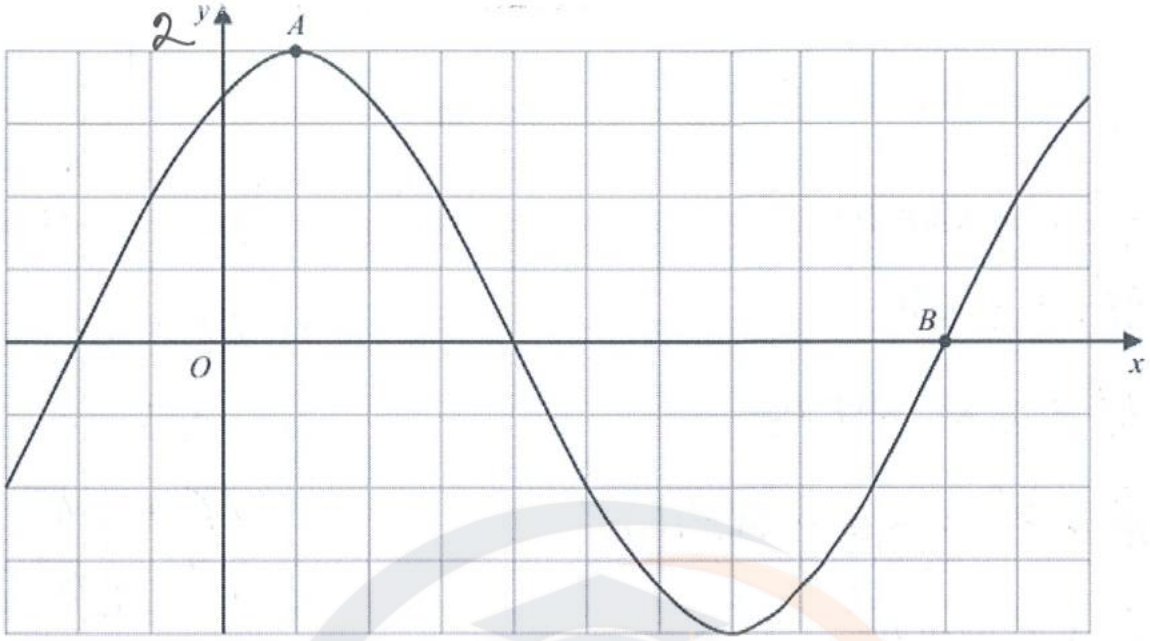
(Total for Question 24 is 6 marks)

Turn over for Question 25

P 7 3 9 Solved by Mr. Pabitra 5 2 8

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25 The diagram shows a sketch of the graph of $y = 2\sin(x + 60)°$



(i) Find the coordinates of the point A

$y = 2\sin(x+60°)$

↙ Amplitude ↙ shifting left by 60°

(30° , 2)

(1)

(ii) Find the coordinates of the point B

(300 , 0)

(1)

(Total for Question 25 is 2 marks)

TOTAL FOR PAPER IS 100 MARKS

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